

# Strength of Materials

---

Tutor

Ashique Ellahi

# Mechanical Properties of Metals

Mechanical Properties refers to the behavior of material when external forces are applied

**Stress and strain**  $\Rightarrow$  **fracture**

For **engineering** point of view: allows to predict the ability of a component or a structure to withstand the forces applied to it

For **science** point of view: what makes materials strong  $\rightarrow$  helps us to design a better new one

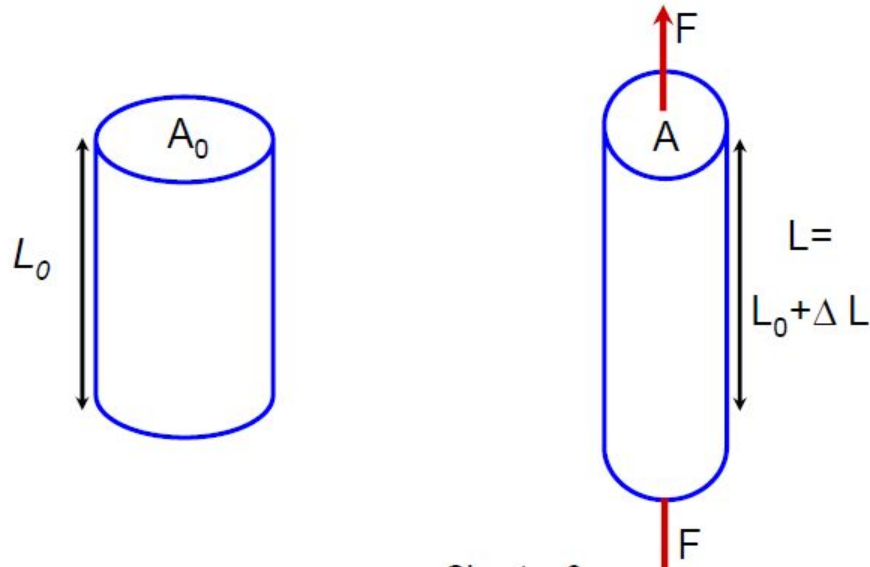
Learn basic concepts for **metals**, which have the simplest behavior

## Main properties of Materials

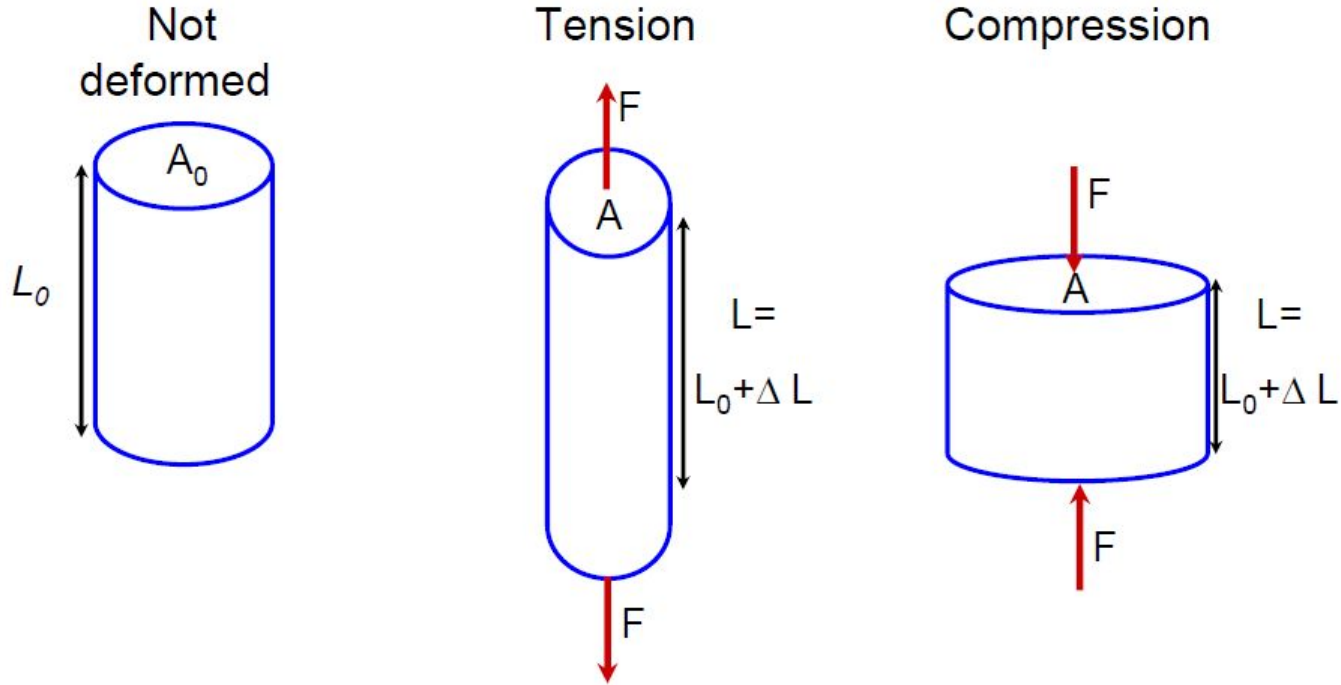
---

- Elasticity
- Plasticity
- Ductility
- Hardness
- Toughness
- Creep
- Fatigue
- Fracture

- Metal piece is subjected to a uniaxial force  $\Rightarrow$  deformation occurs
- When force is removed:
  - metal returns to its original dimensions  $\Rightarrow$  **elastic** deformation (atoms return to their *original position*)
  - metal deformed to an extent that it cannot fully recover its original dimensions  $\Rightarrow$  **plastic** deformation (shape of the material changes, atoms are *permanently displaced* from their positions)



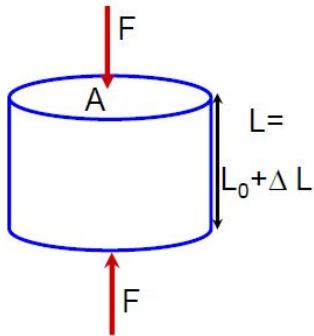
Load can be applied to the material by applying axial forces:



$\Delta L$  can be measured as a function of the applied force; area  $A_0$  changes in response

# Stress ( $\sigma$ ) and Strain ( $\varepsilon$ )

Block of metal



## Stress ( $\sigma$ )

- defining F is not enough ( F and A can vary)
- Stress  $\sigma$  stays constant

$$\sigma = \frac{F}{A}$$

- Units

Force / area = N / m<sup>2</sup> = Pa  
usually in MPa or GPa

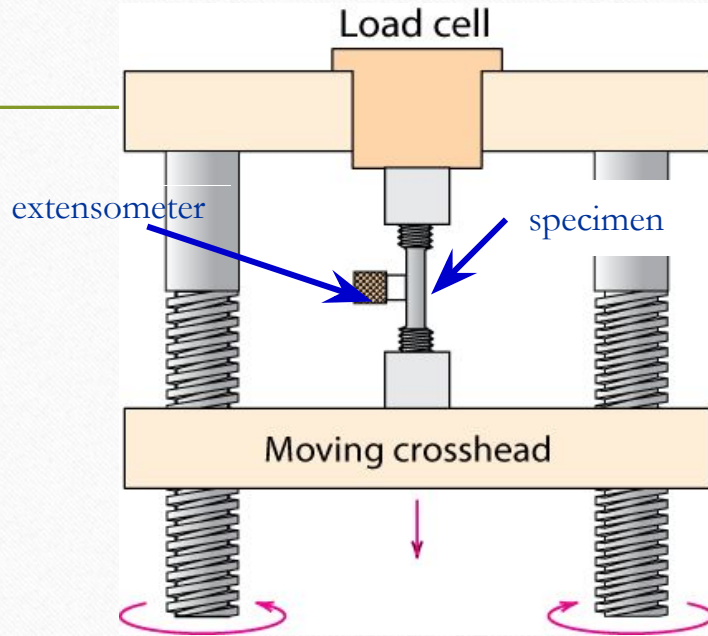
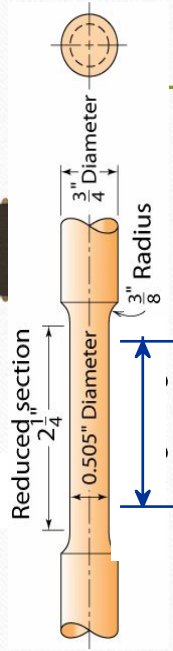
## Strain ( $\varepsilon$ ) – result of stress

- For tension and compression: change in length of a sample divided by the **original** length of sample

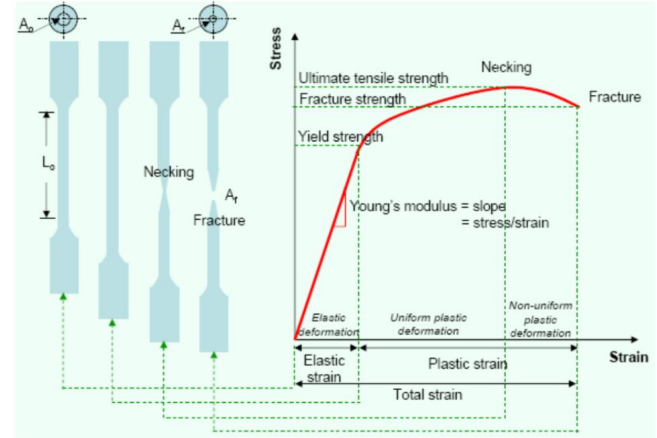
$$\varepsilon = \frac{\Delta L}{L}$$

# Stress-Strain Testing

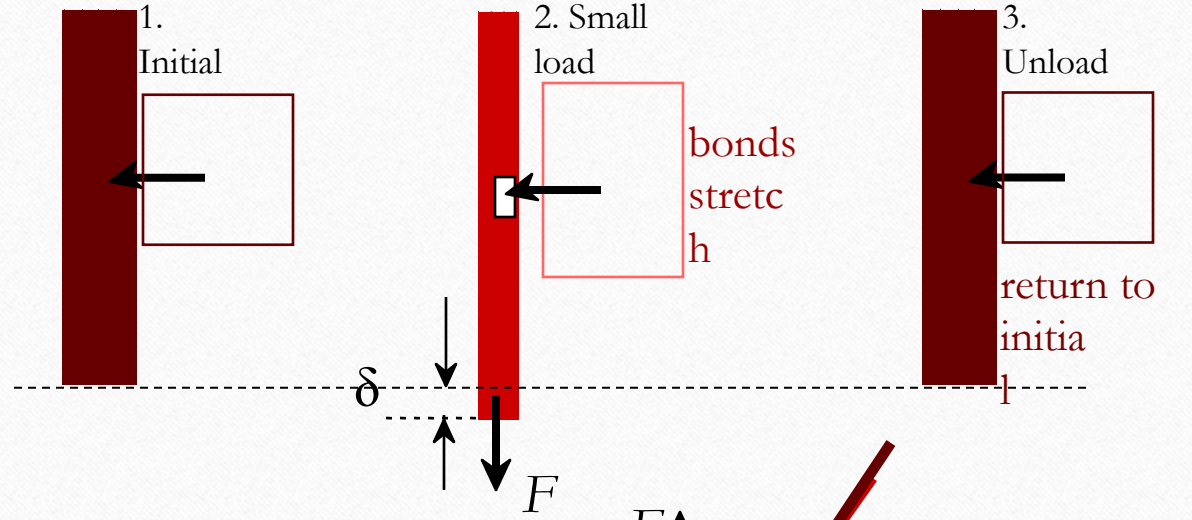
- Typical tensile specimen
- Typical tensile test machine



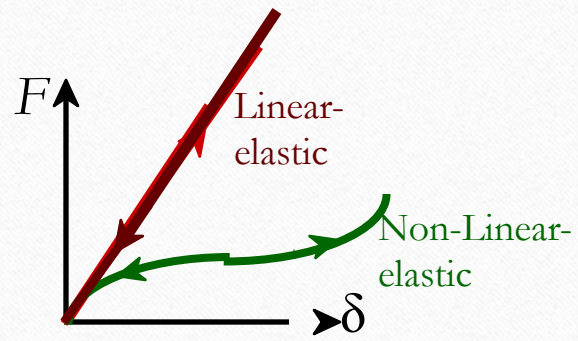
## Tension Test



# Elastic Loading

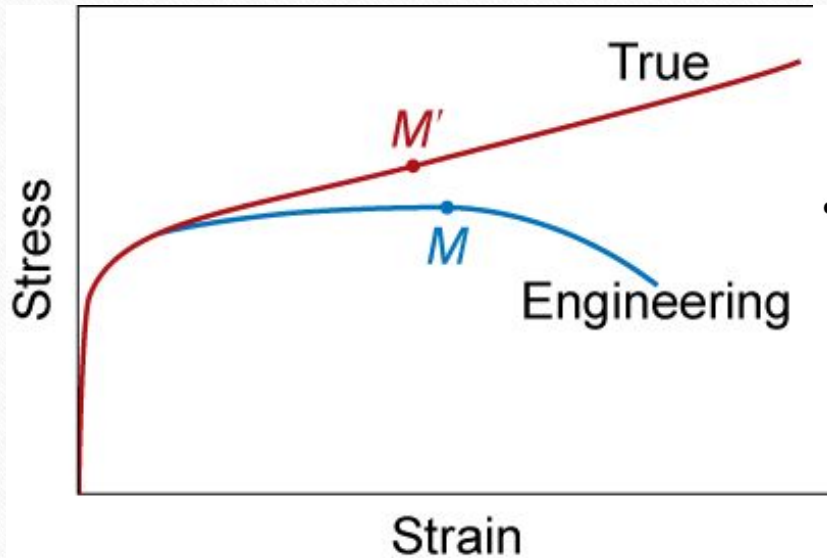


Elastic means reversible!





# True Stress & Strain



The true stress is defined as the ratio of the load to the cross section area at any instant.

$$(\sigma_T) = \frac{\text{load}}{\text{Instantaneous area}} = \sigma(1 + \epsilon)$$

Where  $\sigma$  and  $\epsilon$  is the engineering stress and engineering strain respectively.

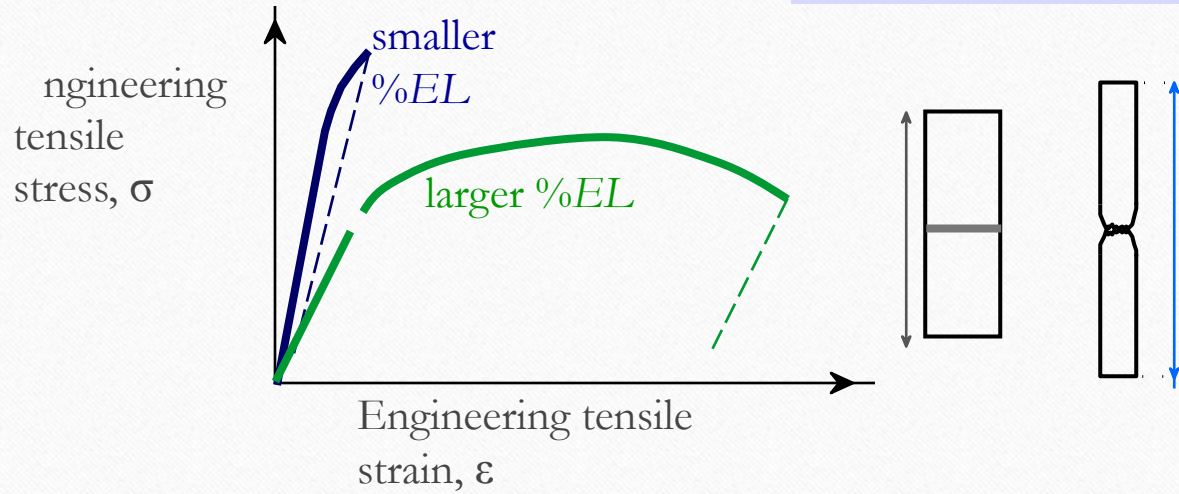
- True strain

$$(\epsilon_T) = \int_{L_0}^L \frac{dl}{l} = \ln\left(\frac{L}{L_0}\right) = \ln(1 + \epsilon) = \ln\left(\frac{A_0}{A}\right) = 2\ln\left(\frac{d_0}{d}\right)$$

# Ductility

- Plastic tensile strain at failure:

$$EL = \frac{x}{100}$$

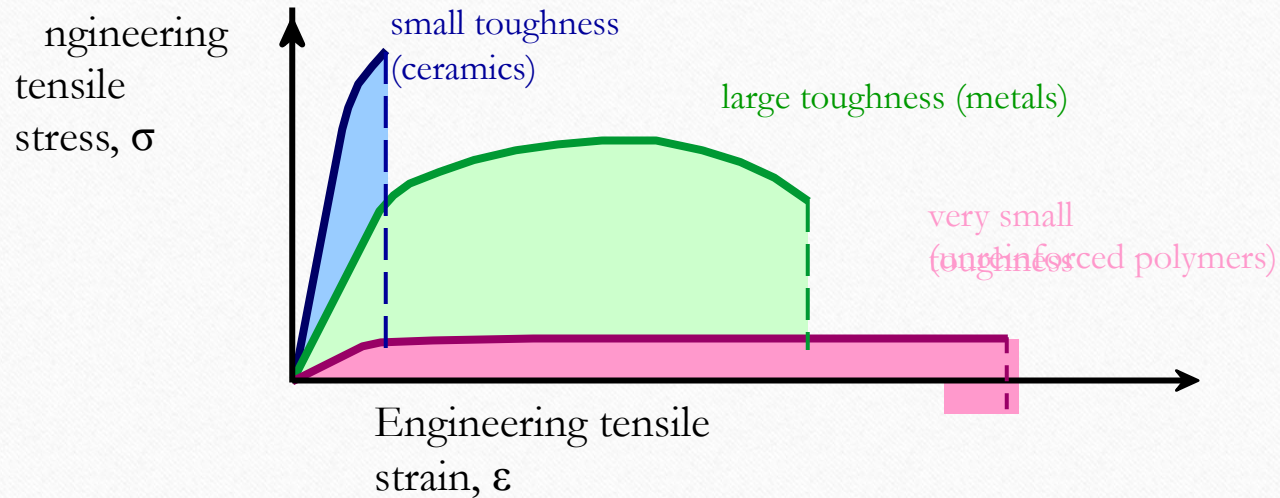


- Another ductility measure:

$$\%RA = \frac{\quad}{100}$$

# Toughness

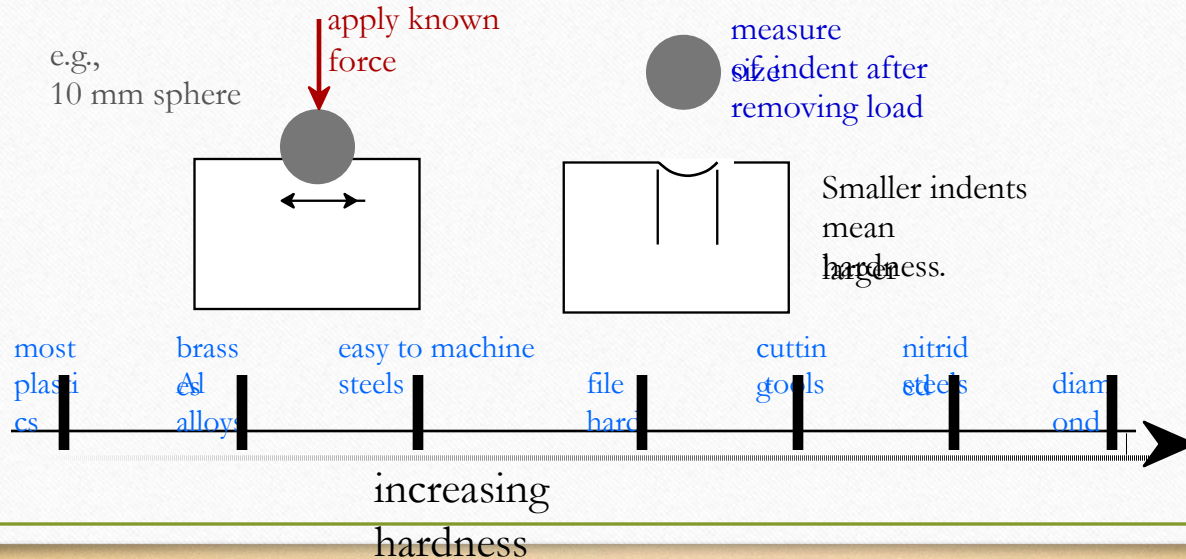
- Energy to break a unit volume of material
- Approximate by the area under the stress-strain curve.



Brittle fracture: elastic energy  
 Ductile fracture: elastic + plastic energy

# Hardness

- Resistance to permanently indenting the surface.
- Large hardness means:
  - resistance to plastic deformation or cracking in compression.
  - better wear properties.



---

Thank You